

# 1<sup>st</sup> order Spatial Statistics

## Holgate Index

The Holgate index is based on the ratio of the distance from a random point to the first and second nearest neighbors. The Holgate are designed to have the same distributions as the Hopkins' indices.

$$Hol_F = \frac{\sum_{i=1}^m d_{(p-t_i)i}^2}{\sum_{i=1}^m d_{(p-t_{2i})i}^2 - \sum_{i=1}^m d_{(p-t_i)i}^2}$$

where  $d_{(p-t_i)i}$  is the distance from a random point to its nearest neighbor tree.  $d_{(p-t_{2i})i}$  is the distance from a tree to its nearest neighbor tree. This test has a F distribution with  $F(2m,2m)$  (Holgate, 1964).

$$Hol_N = \frac{1}{m} \sum_{i=1}^m \left[ \frac{d_{(p-t_i)i}^2}{d_{(p-t_{2i})i}^2} \right]$$

This index has a Normal null distribution  $N(1/2, 1/12m)$ .

- As  $Hop_N$  approaches 0 it indicates a more "uniform" pattern.
- As  $Hop_N$  approaches 1 it indicates a more "clustered" pattern.
- A value of 0.5 is consider random

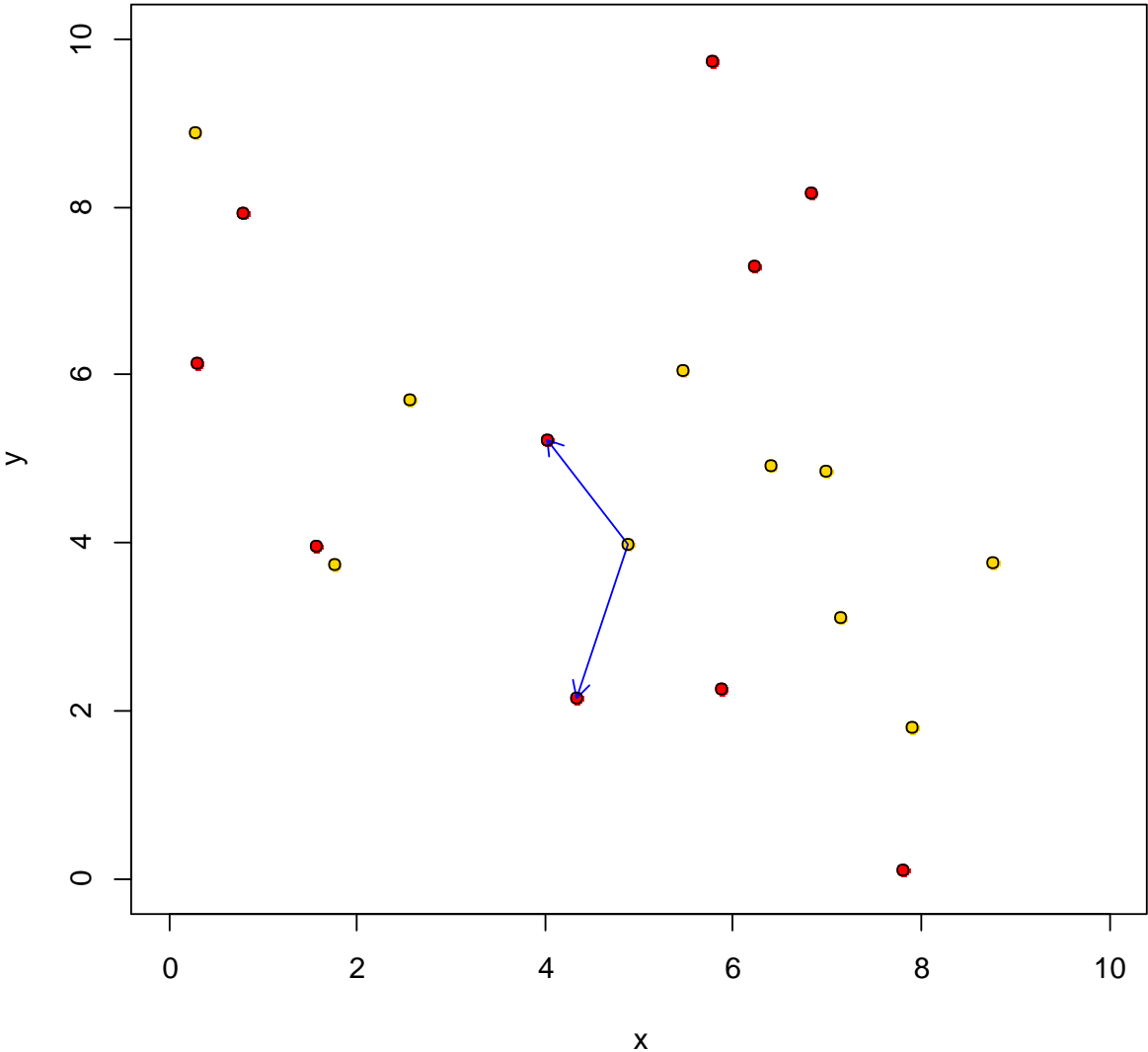


Figure 1. Example of how the Hopkins data is collected. The red dots are trees. The gold dots are random points. We collect the 1<sup>st</sup> and 2<sup>nd</sup> nearest neighbor trees to the point distances.



## Natural Resource Biometrics

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### Also See:

**Hopkins, B.** 1954. A new method for determining the type of distribution of plant individuals. *Annals of Botany* 18:213-227.

**Holgate, P.** 1964. The efficiency of nearest neighbor estimators. *Biometrics* 20:647-649.

**Holgate, P.** 1965. Some new tests of randomness. *Journal of Ecology* 53:261-266.

**Byth, K. and B. D. Ripley.** 1980. Sampling spatial patterns by distance methods. *Biometrics* 36:279-284.

